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Summer Scholars Mathematics Rising 8th Grade

Management Guide pages

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- How to Use This Resource pages (6 pages)
- Grade Level Details pages (7 pages)

Teacher's Guide pages

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Management Guide Rising 7th and Rising 8th Grades





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Using Summer Scholars

How to Use This Resource

The *Summer Scholars Mathematics* curriculum has been designed to meet the needs of summer learning programs. Scaffolded lessons, mathematical discourse, and STEAM activities are presented in a flexible format to make learning (and teaching) fun and effective for everyone.

Student Guided Practice Book

What's Included?

Teacher's Guide



The daily lessons enhance instruction with research-based mathematics instructional practices.



This book encourages students' mathematical fluency with multiple opportunities to apply learning.

Management Guide



This guide helps teachers plan effectively with flexible lesson pacing and a scope and sequence designed specifically for varied summer settings.

12 Mathematical Discourse Task Cards



These cards provide rich problem-solving tasks for students to solve and discuss collaboratively. They are provided in both print and digital format.

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Digital Resources



These resources increase student engagement and enhance instruction. Family Engagement Letters are provided for a strong school-home connection.

Smithsonian STEAM Readers



These books and the included STEAM challenges foster content-area literacy and encourage students to collaboratively solve real-world problems.

Classroom Library with 10 Books



These mathematics- and science-focused books inspire curiosity and a love of reading.

Scaffolded Mathematics Instruction

The student-centered Gradual Release of Responsibility model is embedded into each of the mathematics lessons. Within every two-day lesson, the responsibility shifts from the teacher (I Do) to the student (You Do).



Using Summer Scholars

How to Use This Resource (cont.)

Mathematical Discourse Task Cards

The Mathematical Discourse Task Cards present rich math problems for students to solve and discuss collaboratively. They include two challenge problems.

<section-header>EXPLANT OF A CONTRACT OF A CO</section-header>	Cards can be displayed for the whole class.
Challenge Problems	Challenge problems ask students to think more deeply about the mathematical concept.
Kai la buding a table. He has 480 inches of og for the table lags. The vood is on iong piece. The length and width are both 2 inches. How long will each table lag be?	
Name: Jackson villa are · The pr · The tr · The pr · The tr · The pr · The tr · The pr · The tr · The · The tr · T	Date: De
in the Student Guided Practice Book for individual use.	decides that he needs to pain the model house. If he uses 2 into a all exposed faces, how much surface area will Jackson end ?
Kai is building a t of wood for the pice. The is 2 modes. How for 12	Like He has do not here bele legs. The two in locs of a manual state of a

STEAM Challenges

There are five STEAM Challenges included in each level of *Summer Scholars*. Each challenge is completed over five days to give students ample time to investigate, test, and retest their ideas. In addition to meeting specific criteria, students are also challenged to improve their work over the five days.



Classroom Library

There are many benefits to wide reading, including an increase in vocabulary development. Reading widely increases listening comprehension and contributes to increased reading comprehension. It can be done through independent reading or through teacher read-alouds. Richard Anderson, Paul Wilson, and Linda Fielding's (1988) research shows that the amount of words read per year greatly increased based on the minutes of independent reading completed per day.

Anderson, Wilson, and Fielding ranked students by the number of minutes they read per day. For example, a student in the 70th percentile read almost 10 minutes per day. These students encountered a little more than 600,000 words per year, while a student in the 90th percentile, who read approximately 21 minutes per day, encountered over 1.8 million words each year. Students who encounter more new words apply the strategies they have been taught, and they start to learn the meanings of new words. All these factors associated with reading widely lead to increased comprehension.

Summer Scholars includes a classroom library of 10 books in each level. While these books can help students read widely, they also cover a variety of math and science topics. This can spark student interest and lead to additional connections in grade-level math concepts.

These books can be used as read-alouds, independent reading, or in small groups. They are a flexible tool that can help teachers tailor *Summer Scholars* to meet their unique needs. These books are also available digitally. See page 53 for more information.



Assessment

Assessment is a critical piece of any intervention or summer school program. *Summer Scholars* includes several opportunities for assessment.

- Each kit includes a preassessment and a postassessment to measure student growth. These assessments are provided in the *Student Guided Practice Book*. They can also be accessed as both Google Forms[™] and Microsoft Forms[®] documents. See below for more information. The pages can be ripped out of the student books to make implementation easier.
- Alignments of the preassessments and postassessments are provided digitally. They show the lesson and standard that each question assesses. This can be used to guide further instruction.
- The activity sheets from the Student Guided Practice Book can be used as formative assessments.
- Quick Check activities provide the teacher with valuable insight, which enables them to better support students.
- The digital games can also be used to monitor student progress and math fluency.

Digital Assessment in Summer Scholars

Digital versions of the preassessments and postassessments are provided as fillable PDFs. They can also be accessed as Google Forms[™] documents and Microsoft Forms[®] documents. Please see page 52 for links to these resources.

Using Google Forms™

The Google Forms[™] version of each assessment is best for use with Google Classroom. The links on page 52 prompt a copy of the assessment to be saved to your Google Drive[™]. From there, a share link can be copied and shared with students to take the assessment from any device that has a web browser and internet connection. Having the assessment in Google Drive[™] allows you to easily collect and analyze student data and results. These results can then be shared with administrators as needed.

Using Microsoft Forms®

The Microsoft Forms[®] version of the assessment is best for use with Office 365 Education. The links on page 52 prompt a copy of the assessment to be saved to your OneDrive account. From



there, a share link can be copied and shared with students to take the assessment from any device that has a web browser and internet connection. Having the assessment in OneDrive allows you to collect and analyze student data and results. These results can then be shared with administrators as needed.

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GUMMER Scholars **Mathematics Rising 8th Grade Grade Level Details**

Rising 8th Grade Scope and Sequence

	Mathematics Ski 60–65 minu	ills and Concepts Ltes per day	Problem-Sol 10–15 r	ving and Discourse minutes per day	STE 45 minute	AM es per day
	Mathematics Focus	Standards	Mathematical Practice and Card Title	Standard	Challenge Title and STEAM Step	Standard
Day 1	Proportional	Recognize, represent, and solve proportional, linear	"~~;/~ ∪n	Look for and express regularity in repeated reasoning. Understand	<i>Amazing Tales of Plant Survival</i> Define the Problem and Make a Plan	Make sense of problems and plan,
Day 2	Relationships	relationships in mathematical and real-world problems.	COOKIES	unat generalizing is a process where specific instances are applied to more than one case.	<i>Amazing Tales of</i> <i>Plant Survival</i> Learn Content, Design, and Build	solve, justify, and evaluate solutions.
Day 3	Representing Proportional	Recognize proportional relationships between quantities and	"Cupcake	Reason abstractly and quantitatively to solve a problem. Understand	Amazing Tales of Plant Survival Test	Use appropriate tools, including real objects
Day 4	Relationships with Equations	represent them as equations when given written descriptions, tables, or graphs.	Equations"	that quantities are numbers with labels of corresponding units.	<i>Amazing Tales of</i> <i>Plant Survival</i> Improve	and techniques, to solve problems.
Day 5		Solve real-world and mathematical problems involving the four operations with rational numbers. Add, subtract,		Look for and make use of structure while solving math problems.	<i>Amazing Tales of</i> <i>Plant Survival</i> Reflect and Share	Apply mathematics to solve problems arising in everyday life, society, and the workplace.
Day 6	solving Problems with Rational Numbers	multiply, and divide rational numbers with procedural fluency. Add, subtract, multiply, and divide rational numbers fluently.	Fasten Your Seatbelts!"	Understand that analyzing structure means to look at how the mathematics in the task is organized to solve.	<i>Plant Reproduction</i> Learn Content, Understand the Challenge, and Brainstorm	Define a simple design problem reflecting the need or want that includes specified criteria for success.

	Mathematics Ski 60–65 minu	ills and Concepts Ltes per day	Problem-Sol	ving and Discourse minutes per day	STE 45 minute	AM es per day
	Mathematics Focus	Standards	Mathematical Practice and Card Title	Standard	Challenge Title and STEAM Step	Standard
Day 7	Solving More	Solve mathematical and real-world problems using the		Reason abstractly and quantitatively to solve a problem Understand	<i>Plant Reproduction</i> Design and Build	Use appropriate tools, including real objects
Day 8	Problems with Rational Numbers	Order of Operations to add and subtract rational numbers with procedural fluency.	"Vacation"	that quantities are numbers with labels of corresponding units.	<i>Plant Reproduction</i> Test and Reflect	and techniques, to solve problems.
Day 9	Adding, Subtracting, Factoring, and	Solve mathematical and real-world problems using the order of operations to	"Backyard"	Look for and make use of structure while solving math problems. Understand that	<i>Plant Reproduction</i> Redesign and Rebuild	Apply mathematics to solve problems arising in everyday
Day 10	Equations	multiply and divide rational numbers with procedural fluency.		analyzing structure means to look at how the mathematics in the task is organized to solve.	<i>Plant Reproduction</i> Retest and Share	life, society, and the workplace.
Day 11	Solve Word Problems	Apply and extend previous understanding of properties of operations to	"Oraan (reatures"	Use appropriate tools strategically to solve problems. Understand	<i>All About the Periodic</i> <i>Table</i> Define the Problem and Make a Plan	Make sense of problems and plan,
Day 12	Numbers	add and subtract linear expressions and expand linear expressions with rational coefficients.		that tools can be physical, such as a ruler, or mental, such as strategic thinking.	All About the Periodic Table Learn Content, Design, and Build	solve, justify, and evaluate solutions.

Rising 8th Grade Scope and Sequence (cont.)

Т

Grade Level Details

Jse appropriate tools, Use appropriate tools, including real objects including real objects or want that includes Apply mathematics ife, society, and the specified criteria for and techniques, to reflecting the need arising in everyday and techniques, to to solve problems Standard design problem Define a simple solve problems. solve problems. workplace. 45 minutes per day success. STEAM All About the Periodic All About the Periodic All About the Periodic and STEAM Step **Challenge Title** Reflect and Share Design and Build Air and Weather Air and Weather Air and Weather Understand the **Fest and Reflect** Challenge, and Learn Content, Brainstorm mprove Table Table Table Test mathematics in the task is means to look at how the nstances are applied to solving math problems. nstances are applied to process where specific easoning. Understand **Problem-Solving and Discourse** easoning. Understand use of structure while process where specific egularity in repeated that generalizing is a egularity in repeated that generalizing is a -ook for and express more than one case. ook for and express more than one case. analyzing structure Standard -ook for and make organized to solve. Understand that 10–15 minutes per day 'Circles in Sports" Mathematical **Practice and Card Title** "Paddleboards" "Video Game Rentals" mathematical context and circumference of a circle, and exploring determining the area to solve problems by eal-world problems inequalities within a reasoning about the two-step equations by reasoning about **Mathematics Skills and Concepts** in mathematical or solve one-variable, circumference and mathematical and /ariable, two-step diameter, to solve Standards Model, write, and Know and apply the formulas for the relationship the quantities. between the Write one-60-65 minutes per day quantities. Equations Containing Mathematics to Represent Word Write Inequalities Circumference of Focus **One Variable**

Problems

Day 16

Grade Level Details

Rising 8th Grade Scope and Sequence (cont.)

Day 13

Day 14

Day 15

Day 18

Area and

Day 17

Circles

eal-world problems.

Rising 8th Grade Scope and Sequence (cont.)

	Mathematics Sk 60–65 min	ills and Concepts utes per day	Problem-Sol 10–15 r	ving and Discourse minutes per day	STE . 45 minute	AM s per day
	Mathematics Focus	Standards	Mathematical Practice and Card Title	Standard	Challenge Title and STEAM Step	Standard
Day 19	Solving for Unknown	Apply formulas to find the area, volume, or missing dimensions	"3D Printing"	Use appropriate tools strategically to solve problems. Understand	<i>Air and Weather</i> Redesign and Rebuild	Apply mathematics to solve problems arising in everyday
Day 20	Ulmensions	of two- and three- dimensional figures.		that tools can be physical, such as a ruler, or mental, such as strategic thinking.	<i>Air and Weather</i> Retest and Share	life, society, and the workplace.
Day 21	Understanding	Understand the validity constraints of random samples,		Construct viable arguments and critique the reasoning of others. Understand how to	<i>Space Technology</i> Define the Problem and Make a Plan	Make sense of problems and plan,
Day 22	Random Samples	and use the data non- a random sample to make inferences about a population.		use evidence to justify thinking and respectfully critique the reasoning of others.	<i>Space Technology</i> Learn Content, Design, and Build	solve, justify, and evaluate solutions.
Day 23	Understanding	Understand the probability of a chance event, and determine the experimental	"semen"	Look for and make use of structure while solving math problems. Understand that	<i>Space Technology</i> Test	Use appropriate tools, including real objects
Day 24	Probability	and theoretical probabilities related to simple and compound events.		analyzing structure means to look at how the mathematics in the task is organized to solve.	<i>Space Technology</i> Improve	and techniques, to solve problems.
Day 25	Culminating Activity				<i>Space Technology</i> Reflect and Share	Apply mathematics to solve problems arising in everyday life, society, and the workplace.

Grade Level Details

Rising 8th Grade STEAM Challenges and Materials

This chart includes descriptions and needed materials for the five STEAM Challenges.

Challenge Name	Description	Materials		
Amazing Tales of Plant Survival	Teams will create models of a newly discovered plant affected by its extreme environment.	 2 paper plates modeling clay construction paper 5 cardboard tubes 	 10 pipe cleaners 10 craft sticks masking tape 10 toothpicks 	
Plant Reproduction	Groups will collaborate to make vehicles for seed dispersal.	 5 cardboard pieces 4 coffee filters handheld fan foil 	lima beans15 pipe cleaners4 ft. of string	
All About the Periodic Table	Teams will design and create mobiles inspired by the periodic table. The mobiles need to be hangable.	 30–50 beads 10 craft sticks masking tape 10 index cards 10 paper clips 	 3 paper plates 10 pipe cleaners pom-pom balls 5 ft. of string 4 wooden dowels 	
Air and Weather	Groups will build parachutes that can unfold or already be in its open position when dropped.	 5 cardboard tubes 4 ft. of string plastic wrap 5 pieces of tissue paper 	 paper clips 2 washers 2 identical items to drop 	
Space Technology	Teams will engineer models of a Mars lander that can safely land a marshmallow when dropped to the ground.	 5 coffee filters 20 craft sticks 10 sheets of tissue paper large paper or plastic cup 	 foil masking tape 6 index cards 5 ft. of string 	

Rising 8th Grade Classroom Library Information

This chart includes important information about the books included in the classroom library.

Book Title	Lexile® Measure	*Guided Reading Level	Summary
All About Mechanical Engineering	770L	Y	Learn about how mechanical engineering is used all around us. Readers will discover things such as velocity, acceleration, rotation, dimensions, measurements used, and Newton's Laws.
Hurricane Hunters: Measures of Central Tendency	920L	V	Learn about measures of central tendency while following the lives and work of hurricane hunters! Read about the instruments that hurricane hunters use and how they analyze the data that these instruments collect.
Investigating Forces and Motion	810L	W	Force and motion are all around us and help us move and do great things! Readers will explore how forces and motions work.
Isaac Newton and the Laws of the Universe	800L	Х	Read about the incredible life of Isaac Newton in this fascinating biography. Learn how Newton researched gravity, acceleration, deceleration, motion, and light spectrum.
Land Animals: Solving Equations and Inequalities	970L	V	Practice solving equations and inequalities while reading about land animals from all over the world! Learn interesting facts about Earth's land animals, discovering how zoologists use variables to solve equations and inequalities, and answer questions about these animals.
Package Design: Surface Area and Volume	920L	W	Learn how designers work with two-dimensional and three-dimensional shapes, measuring their surface area, volume, diameter, and radius, to create great package designs!
Tonight's Concert: Using Data and Graphs	940L	W	Learn how to read and construct statistical graphs and prepare for a concert! Master bar graphs, circle graphs, line graphs, histograms, and line plots.
What Did I Eat?: Fractions, Decimals, and Percents	870L	V	Learn about the ingredients and nutrients of various foods while practicing mathematical operations with fractions, decimals, and percentages!
Where Germs Lurk: Simplifying and Evaluating Expressions	860L	W	Write, simplify, and evaluate algebraic expressions to explore how quickly germs can spread! Learn all about germs and how they spread, encouraging healthy habits, while allowing students to practice algebraic expression, exponential form, and distributive property.
The Wonder of Outer Space	780L	S	Come explore the wonders of space! From satellites to space food, observatories to Sputnik, readers will learn all about space and the various ways people have explored and learned about astronomy for years!

*These titles have been officially leveled using the F&P Text Level Gradient™ Leveling System.



Teacher's Guide

Rising 8th Grade



Days 1–2 Overview

Proportional Relationships

Learning Outcome

• Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.

Focus

This lesson will address this focus question: *How do you know if two quantities are in a proportional relationship when given a table or graph?* You may wish to write the focus question on the board or chart paper and read it aloud to students.

Teacher Background

Proportional thinking prepares students for higher-level mathematics. The progression from linear equations and graphs to quadratic equations and graphs starts with proportional thinking. Students may have difficulty setting up ratios and finding equivalent ratios. Creating a table and/or graphing the ordered pairs can help students determine if there is a proportional relationship. Students may also draw models of each ratio to explain their reasoning.

Mathematical Discourse

Learning Outcome

• Look for and express regularity in repeated reasoning. Understand that generalizing is a process where specific instances are applied to more than one case.

Amazing Tales of Plant Survival

Learning Outcome

• Use mathematical knowledge to define an engineering problem and design solutions.

STEAM Vocabulary

adaptations carnivorous cloning native photosynthesis pollen

Materials

- Student Guided Practice Book (pages 4–14)
- Amazing Tales of Plant Survival book

Cookies task card

chart paper markers

*You may wish to assemble one set of STEAM materials for students to reference (see page 10).

Proportional Relationships

Warm-Up 🎬 🗓

1. Write the following problem and table on the board or chart paper: Janie is bringing cupcakes to a bake sale. She charges \$1.50 for two cupcakes. What is the unit price of the cupcakes? How much will 15 cupcakes cost?

cupcakes	2	4	6	12	15
price	\$1.50	\$3.00	\$4.50	\$9.00	?

- 2. Ask, "How can we find the unit price of the cupcakes?" (*Write a complex fraction for price/cupcakes.*) Remind students to find the unit price by dividing the numerator by the denominator. Ask, "How do you divide fractions?" (*Multiply the first fraction by the reciprocal of the second fraction.*) Have students work with partners to solve the problem. Students should find that the unit price for one cupcake is \$0.75 by dividing \$1.50 by 2.
- **3.** Ask students, "How do you find the cost of 15 cupcakes?" (*Multiply 15 by the unit price*, \$0.75, which is \$11.25.)

Language and Vocabulary

1. Prior to the lesson, write the following vocabulary terms on the board or chart paper:

equivalent ratio ordered pairs origin

proportional relationship

- 2. Have students create working definitions of the terms based on their previous experience with them. Provide students with markers and chart paper. During the lesson, have students revise and/or add to their definitions.
- **3.** Review the definitions with students. A proportional relationship exists if the ordered pairs (*x*, *y*) in a table are equivalent ratios and the graph will pass through the origin and make a straight line on a coordinate plane.

Proportional Relationships

I Do 🗯 15

- 1. Say, "Today, we are going to look at tables and graphs to determine if there is a proportional relationship."
- 2. Say, "We will start by looking at a table." Write the following table on the board or chart paper.

bananas (x)	5	10	15	20
cost (y)	\$1.00	\$2.00	\$3.00	\$4.00

- Say, "To determine if there is a proportional relationship, we have to see if the ordered pairs in the table are equivalent ratios." Ask, "What patterns do you see in this table?" Allow students to discuss their ideas with partners and share. Students may indicate that for every group of 5 bananas, the cost increases by \$1.00.
- 4. Ask, "How do we find the unit rate?" (Divide the cost by the number of bananas.) Say, "Let's divide \$1.00 by 5 to see what the cost of one banana is. When thinking of money, if I share \$1.00 into 5 groups, how many cents will be in 1 group?" (\$0.20) Ask, "So, what is the unit rate?" (The cost per one banana is \$0.20.) Have students check that the unit rate is true for all the ordered pairs by multiplying the unit cost by the number of bananas to find the total cost. Say, "Since all of the ratios are equal, the table shows a proportional relationship."

5. Say, "Let's graph the ordered pairs from the table. When graphing, remember to start at the origin (0, 0). For the *x*-coordinate, move left or right along the *x*-axis, and for the *y*-coordinate, move up or down along the *y*-axis." Display the following graph.



6. Say, "Notice that the points (when connected) form a straight line that passes through the origin (0, 0). This graph is an example of a proportional relationship."

Support for Language Learners: Each time you use the terminology *proportional relationship, equivalent ratio, ordered pairs,* and *origin,* point to them in the problem. This will allow students to associate the verbal word with the visual representation. For example, as you discuss the origin, point to (0, 0) on the coordinate plane to emphasize the word and the example.

Proportional Relationships

We Do ((15)

1. Display *Painting Ratios* on page 4 of the *Student Guided Practice Book.* Say, "Let's look at another table together." Display the table for Question 1:

yellow	4	6	8	10
blue	8	12	16	

- 2. Ask, "How can we determine if the ratios in the table are equivalent?" (Look for a pattern within the numbers.) Ask, "Are these equivalent ratios?" (Yes.) "How do you know?" (The number of ounces of blue paint is double the amount of ounces of yellow paint.) Ask, "Does this table show a proportional relationship?" (Yes, because the ratios are equivalent.) Ask, "How do we find the number of ounces of blue paint needed for 10 ounces of yellow paint?" (Multiply 10 and 2, which is 20.)
- **3.** Say, "Now, let's determine if there is a proportional relationship by looking at a graph." Display the table for Question 2:



4. Ask, "How can we determine if this graph shows a proportional relationship?" Allow students to discuss with partners, and then ask for volunteers to share with the class. Students should agree that the graph of a proportional relationship must start at the origin (0, 0) and that the points must form a straight line. Ask, "Does this graph show a proportional relationship?" (*Yes, the graph satisfies both conditions.*)

- **5.** To help students explain their reasoning, provide them with the following sentence frames.
 - For a table to show a proportional relationship, the ____ must be ____. (ratios; proportional)
 - For a graph to show a proportional relationship, it must pass through the _____ and the points must form a _____ (origin (0, 0); straight line)

You Do 🖁 🛄

- 1. Have students complete *Baking Proportions* from page 5 of the *Student Guided Practice Book.* Encourage students to remember that a proportional relationship can be determined by proportional ratios and graphed so that ordered pairs pass through the origin and are in a straight line.
- 2. Have students share their solutions and reasonings. If students have difficulty explaining their reasonings, remind them to use the sentence frames and vocabulary terms.

Cookies



Math Skill–Proportional Relationships

Students will build on their prior knowledge of unit rates, ratios, and analyzing graphs to understand what proportional relationships are and how they function. They will use their understanding of proportional relationships to solve problems in a variety of ways.

Support for Language Learners:

Mathematical terms, such as *ratio* and *rate*, can be challenging to learn. They sound similar but have different meanings. Support students by creating a visual chart that includes vocabulary words, definitions, and examples of these terms for students to reference.

Procedure 🛱 🛅

- Make the math real for students. Remind them that proportional relationships can be determined if you have graphs or tables of values. For a graph, a proportional relationship is observed with a straight line through the origin (0, 0). For a table, a proportional relationship is indicated when each value of the ratio is divisible by the same number.
- 2. Display the *Cookies* task card, and read aloud the text. Give students the opportunity to ask clarifying questions before starting the task.
- **3.** Provide time for students to collaborate with partners to complete the task from page 6 of the *Student Guided Practice Book*. (Students will complete the challenge problems on the next day of instruction.)
- 4. Have partners discuss the Discourse Prompts.

Discourse Prompts

- How is the *Cookies* task related to unit rate?
- How would you teach a classmate who missed today's lesson to determine if two variables are proportional?

Lesson Support

Answer: The number of cookies is not proportional to the cost. **Note:** Some students may notice that the cost of 6 cookies is proportional to the unit rate. You would pay \$1.17 per cookie if you purchased 12 cookies.

Possible Student Misconception: Look for students who have difficulty comparing values to determine if they are proportional. Remind them to be consistent when writing proportions (e.g., cookies:cost or cost:cookies).

Amazing Tales of Plant Survival

Materials and Preparation

• Prepare a set or list of supplies to show students (5 cardboard tubes, construction paper, 10 craft sticks, masking tape, modeling clay, 2 paper plates, 10 pipe cleaners, 10 toothpicks).

Read Aloud 🎬

- 1. Draw a two-column chart on the board or on chart paper with one column titled *What Plants Provide* and the other column titled *What Plants Require.* Invite students to share their ideas aloud to complete the chart. To activate their thinking about plants surviving in harsh environments, ask students to suggest how plants may respond if an aspect of what plants require was limited or unavailable. Ask students which of Earth's environments may be considered harsh for plant survival and why.
- 2. Read aloud a few pages of the Amazing Tales of Plant Survival book to students. While reading, have them continue to document new information about plants on the two-column chart.

Define the Problem 🛱 🎬

- Have students work in pairs to create sketches of plants living in their native environments. Ask students to include as many features of the plants as they can think of based on their prior knowledge and new information from the text. Encourage students to add details to their plant sketches, including shapes of leaves, root structures, and plant height.
- 2. Reveal the STEAM challenge by reading aloud pages 28–29 of the book. Students can follow along on page 7 of the *Student Guided Practice Book*.

- **3.** Refer students to *Make a Plan* on page 8 of the *Student Guided Practice Book*. Have students write quick summaries of the challenge with partners. Summaries should include constraints and criteria.
- **4.** Have students complete the My Design portion of the page independently. Students will complete the Team's Design section on the next day of instruction.

Vocabulary Activity 🕅 🗓

- Write the vocabulary words (adaptations, carnivorous, cloning, native, photosynthesis, pollen) on the board or chart paper. Ask students to suggest definitions for any words they are familiar with, including parts of a word such as adapt in the word adaptations. Have students provide a context of where they have used each word.
- 2. Discuss with students the meaning of each vocabulary word, and record definitions. Have students work in pairs to use each of the words correctly in a sentence. Invite students to share their sentences aloud.

Proportional Relationships

Progress Monitoring 🖁 5

- 1. Have students complete *Quick Check* on page 9 of the *Student Guided Practice Book* to gauge student progress toward mastery of the learning outcomes.
- 2. Based on the results of the *Quick Check* and your observations during the lesson, identify students who may benefit from additional instruction in the learning outcomes.

Rotations 🎬 🖁 🧓

Place students in two groups. Work with one group on the Refocus activity while the other group completes the Practice activity. Rotate after 15 minutes. Work with the second group on the Extend activity while the first group completes the Practice activity.

Refocus 🗰

1. Write the following table on the board or chart paper:

chores	1	2	3	4	5
earnings					

Say, "Pretend your parent is going to pay you \$1.00 for each chore you do. Let's complete the table to find your earnings." Guide students in completing the table. Ask, "What is the unit rate?" (*\$1.00 per chore*) "How much will you earn if you do two chores?" (*\$2.00*) "What is the repeating pattern?" (*Multiply the number of chores by \$1.00*.)

- 2. Once you have completed the table, have students complete tables independently if the unit rate is \$5.00 per chore.
- **3.** If time allows, support students as they complete Question 1 from *Refocus* on page 10 of the *Student Guided Practice Book*. If not, students will complete both problems from this page during the Practice activity.

Extend 📅

- 1. Support students as they complete *Extend Learning Task* on page 11 of the *Student Guided Practice Book.*
- 2. Students will create their own tables and graphs that represent a proportional relationship. Ask students to choose topics for the *x* and *y*-coordinates and create a repeating pattern to complete the table. Then, they will graph their ordered pairs on the coordinate plane. Finally, have them exchange their work with partners who will determine if their table and graph represent a proportional relationship.

Practice ရှိ

- **Refocus Group Practice:** Have students complete the questions on *Refocus* on page 10 of the *Student Guided Practice Book* to reinforce their learning.
- Extension Group Practice: Have students complete Independent Practice on page 12 of the Student Guided Practice Book to reinforce their learning.

Proportional Relationships

Math in the Real World 🎬 🛱 🔁

- 1. Display Math in the Real World: Planting Time from page 13 in Student Guided Practice Book. Have a student read the task aloud. Tell students to explain or summarize the task to their partners. Have a few students share their summaries.
- 2. Ask students to think about what information they will need to complete the task and what the task is asking them to do. Then, have them share with partners. Ask a few students to share. Students should indicate that they know some of the ordered pairs in the table and can use that information to find the pattern and complete the table so that it represents a proportional relationship. They need to complete the table, find the unit ratio, and decide if the owner is right or wrong. Have students work in groups of two or three to complete the task.
- **3.** As students are working, circulate, and ask focusing, assessing, and advancing questions.
 - What are you trying to find out?
 - How do you know if the table represents a proportional relationship?
 - What is the unit ratio for this table?

Support for Language Learners: Share these sentence frames to help students explain their reasonings.

- I completed the _____ by _____.
- The table represents a _____ because
- The unit ratio is _____ because _____

- 4. Observe how students are solving the task, and choose a few groups who solved the task in different ways to share their solutions and reasonings. Students should find that the unit ratio is 3 bean plants for every 1 sunflower. Students should complete the table by multiplying the number of sunflowers by 3 to find the number of bean plants. They should understand that the table represents a proportional relationship. The owner of the nursery is incorrect. The ratio of sunflowers to bean plants in the table is 1:3, not 3:1.
- **5.** As groups share their solution paths, reasonings, and strategies, ask the following questions.
 - Do you agree or disagree with the solution path and reasoning? Why?
 - Who can restate <u>'s strategy/solution</u> path/reasoning?
 - Which solution path makes the most sense to you? Why?

Mathematical Discourse

STEAM Challenge

Cookies

Challenge Problems 🛱 🛅

- 1. Provide time for students to complete the *Cookies* task from the previous day of instruction.
- 2. Have pairs of students work together to complete the challenge problems.

A cookie recipe requires $3\frac{1}{2}$ cups of flour to make 5 dozen cookies. How much flour is needed to make 4 dozen cookies? **Answer:** $2\frac{4}{5}$ cups of flour If a 10-pound turkey takes 4 hours to cook in the oven, how long would it take to cook a 16-pound turkey? **Answer:** $6\frac{2}{5}$ hours

Amazing Tales of Plant Survival

Materials and Preparation

• Prepare a set or list of supplies to show students (5 cardboard tubes, construction paper, 10 craft sticks, masking tape, modeling clay, 2 paper plates, 10 pipe cleaners, 10 toothpicks).

Read Aloud 🚟

- 1. Ask a volunteer to share a quick, onesentence summary of what was read yesterday in the *Amazing Tales of Plant Survival* book.
- 2. Continue reading aloud from the book for about five minutes. Pause periodically to discuss new information and answer any questions students may have.

Science Connection \mathfrak{m}

- Ask students to envision themselves as botanists who have been asked to deliver a presentation about a plant adaptation at a scientific conference.
- 2. Have students work in pairs to prepare information needed for the presentation on *You're the Expert* from page 14 of the *Student Guided Practice Book.*

Design 🛱 🗓

- 1. Organize students into teams, and ask teams to have members share the designs they created on the previous day of instruction using *Make a Plan* from page 8 of the *Student Guided Practice Book.*
- Have groups choose, sketch, and label team designs on the Team's Design section on *Make a Plan*. Each team should incorporate ideas from individual students' designs. (Team designs must be submitted for teacher approval before building begins.)
- **3.** Tell students they will build models of their team designs on the next day of instruction.



Student Guided Practice Book

Rising 8th Grade



Painting Ratios

Directions: Solve the problems.

1 An art teacher has a table of yellow paint and blue paint to mix to get a certain hue of green. Does the table show a proportional relationship between yellow and blue? Explain your solution. If so, complete the table.



2 Jean draws a graph that shows the amount of red and yellow paint to mix to get a certain hue of orange. Does her graph show a proportional relationship? Explain your solution.



Baking Proportions

Directions: Solve the problems.

1 Cara shows the number of cookies and cupcakes she sells at the bake sale each hour in the table below. She says that she always sells the cupcakes and cookies in the same proportion. Is Cara correct? Explain your solution.

Cupcakes	Cupcakes 3		9	12	
Cookies	Cookies 6		18	21	

2 The graph below shows the cost of a given number of books. Does the graph show a proportional relationship? Explain your solution.



5

Name: _

Name:

Day 1

Date:



Cookies

Liem goes to a bakery to buy cookies for a party. Determine whether the relationship between the cookies and cost is proportional or nonproportional. Explain how you know.

Cookies	Cost
1	\$1.50
6	\$9.00
12	\$14.00
24	\$26.00

If Liem purchases 12 cookies, how much is he paying for each cookie?



Challenge Problems

A cookie recipe requires $3\frac{1}{2}$ cups of flour to make 5 dozen cookies. How much flour is needed to make 4 dozen cookies? If a 10-pound turkey takes 4 hours to cook in the oven, how long would it take to cook a 16-pound turkey?

6



Define the Problem

As a botanist, you are constantly exploring extreme environments looking for new plant species. You recently discovered an amazing new plant but were unable to remove any samples from the environment. Your camera was also affected by the extreme conditions, so no photographs of the plant exist. However, you need to share information about it with other scientists. Your task is to create a model of your newly discovered plant species to share with others.



Constraints: You may only use the materials provided to you. Your newly discovered plant must live in a real and extreme environment on Earth.

Criteria: Your model plant must show the adaptations that allow it to survive in the extreme environment where it lives. The model plant must show how it protects itself from being eaten and how it protects itself from the weather. The model must also show the unique way it reproduces. You may include any other unique adaptations.



Research and Brainstorm

What are some extreme environments on Earth, and where did you discover this new plant species? What are some adaptations of other plants that help them in extreme environments? What special structures or behaviors could your plant have to help it survive? Which materials will work best for your model?



Design and Build

Sketch two or more designs for your plant model. Label the parts and the materials. Choose the design you think will best meet the criteria. Then, build your plant model.



Fest and Improve

Share your model with others. Explain where it was discovered. Explain its special structures and behaviors that help it survive. How can you improve it? Will you set any new goals for your design? What are they? Modify your design and reassess how well it meets the criteria.



Reflect and Share

What about this challenge did you find most interesting? How did you apply your scientific knowledge to complete this challenge? How can models be helpful?

Day 1

Date:_____

Make a Plan

Directions: Summarize the challenge. Then, sketch your design to solve the challenge.

Challenge: _____

My Design

Directions: Sketch your team's design. Label the materials needed.

Team's Design



Quick Check



 Jason is mixing red and blue paint to get different hues of purple. Does his table show a proportional relationship? Choose yes or no. Explain your answer.



2 Judie posts a table to show how many cups of dried fruit and nuts go into batches of trail mix. Does the table show a proportional relationship? Choose yes or no. Explain your answer.

Dried fruit	2	4	6	8	Yes
Nuts	6	12	24	32	No

Harry draws a graph of how many miles the drivers for his trucking company should be driving over the course of one week.

Does the graph show a proportional relationship? Explain your answer.





Directions: Do the tables show proportional relationships? Explain your solutions.

Image a table of the number of days he runs and the miles he runs.
Days 5 7 8 10 12
Miles 30 42 48 60 72

Smoothies	3 4		6	8	9	
Price	\$9.00	\$12.00	\$24.00	\$32.00	\$81.00	

Extend Learning Task

Directions: Create a table and graph that represents a proportional relationship.



Name: _____

Independent Practice

Directions: Does each table show a proportional relationship? Explain your solutions.

5	7	8	9	10
20	28	32	36	40
	r — — ¬			
4	5	7	9	10
	20	19	63	70

Directions: Does the graph show a proportional relationship? Explain your solution.





Planting Time

The table shows a guide for planting flowers and vegetables in a garden nursery. Some of the numbers were washed away during a rainstorm. Complete the table so that it represents a proportional relationship.

Sunflowers	8	18	30		36	42		55
Bean Plants		54		96		126	135	165

- **A.** What is the unit ratio?
- B. The owner of the nursery says that if there are 180 bean plants planted, there should be 540 sunflowers planted. Is she right or wrong? Explain your solution.



You're the Expert

Directions: Choose a plant from the book to investigate.

Name the plant, and describe or show where it's found.

List features of the environment that make it hard for the plant to survive.

Draw a picture to show the plant's adaptations in this environment. Label the adaptations.

Include a fun fact or interesting feature about this plant.